

Implementing ODA from Within Stata: Assessing Split-Half Reliability Using a Polychotomous Attribute

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This paper illustrates testing a directional (i.e., confirmatory) hypotheses for a split-half reliability study using a polychotomous attribute having four categories, via the Stata package for implementing ODA.

Recent papers¹⁻²⁵ introduce the new Stata package called **oda**²⁶ for implementing ODA from within the Stata environment. This package is a wrapper for the MegaODA software system²⁷⁻²⁹, so the MegaODA.exe file must be loaded on the computer for the **oda** package to work.³⁰ To download the **oda** package, at the Stata command line type: “ssc install oda” (without the quotation marks).

Using the split-half method to estimate reliability requires only one test administration. Items on the test are separated into two groups called “split-halves” and the agreement between the split-halves is corrected for attenuation and called the split-half reliability for the total test. Every person completing a pair of split-halves is hypothesized to receive identical scores on both split-halves.³¹

This paper demonstrates use of the **oda** package to evaluate a directional hypothesis for a design in which two split-halves are separately used to categorize a sample of undergraduates into one of four mutually exclusive categorical

typologies: androgynous (dummy-coded as 1), instrumentally-typed (2), expressively-typed (3), or undifferentiated (4).³¹⁻³⁹

Methods

Data

Yarnold obtained data assessing instrumentality and expressiveness (each using 20 items) for 68 undergraduates.³² The 20 “I” items were randomly split into two halves (I_1 and I_2), as were the 20 “E” items (E_1 and E_2). Separately using each pair of split-halves (I_1, E_1) and (I_2, E_2), each undergraduate was classified into one of the four dummy-coded categorical typologies. Finally, separately for every undergraduate, the categorical typology (1-4) was determined for the first and second split-half.

Analytic Process

We test the directional (“confirmatory”) alternative hypothesis that subjects classified as type t

($t = 1, 2, 3,$ or 4) by split-half 1 (four-category class variable) are similarly classified by split-half 2 (four-category “polychotomous” attribute). The null hypothesis is this is not true.^{30,40} Analysis was accomplished using the following **oda** syntax (see the help file for **oda** for a complete description of syntax options):

```
oda sh1 sh2, pathoda("C:\ODA\")
store("C:\ODA\") iter(25000)
direction(< 1 2 3 4) cat
```

This syntax is explained as follows. Here “sh1” is the polychotomous *class* variable and “sh2” is the polychotomous *attribute*; the directory path where MegaODA.exe and other files generated in analysis are stored is “C:\ODA\”; 25,000 iterations (repetitions) are used to obtain a permutation p -value; and the directional hypothesis is that polychotomous codes of the class variable and attribute are identical.²⁶ The **oda** package produces an extract of the total output produced by ODA software seen below (the complete output is stored in the specified directory with the extension “.out”).

```
ODA model:
-----
IF SH2 = 1 THEN SH1 = 1
IF SH2 = 2 THEN SH1 = 2
IF SH2 = 3 THEN SH1 = 3
IF SH2 = 4 THEN SH1 = 4

Summary for class SH1 Attribute SH2
-----
Performance Index          Train
-----
Overall Accuracy          64.71%
PAC SH1=1                 73.33%
PAC SH1=2                 61.11%
PAC SH1=3                 68.42%
PAC SH1=4                 56.25%
Effect Strength PAC       53.04%
PV SH1=1                 64.71%
PV SH1=2                 61.11%
PV SH1=3                 81.25%
PV SH1=4                 52.94%
Effect Strength PV        53.34%
Effect Strength Total     53.19%

Monte Carlo summary (Fisher randomization):
-----
Iterations: 25000
Estimated p: 0.000000
```

As seen, the classification performance of the ODA model corresponds to a statistically significant (conventionally reported as per-comparison $p < 0.0001$) effect. Effect strength for sensitivity (ESS) is labelled in the output as “Effect Strength PAC” (Percentage Accurate Classification). For the confirmatory hypothesis ESS is 53.04%, which barely exceeds the minimum criterion ($ESS \geq 50$) for classification as a relatively strong effect.³¹ But, an exact discrete confidence interval for this result would overlap the region reflecting a moderate effect.^{41,42}

Classification performance of the ODA model is summarized in a cross-classification table, illustrated for this example below.

Actual Class	Predicted Class				PAC (%)
	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	
1	11	2	2	0	73.33
2	3	11	0	4	61.11
3	2	0	13	4	68.42
4	1	5	1	9	56.25

Here, PAC is “percentage accuracy in classification,” also called model sensitivity.³¹ Since there are four class categories, sensitivity of $100\%/4 = 25\%$ is expected by chance for each of the four categories. Best performance was achieved for class 1 (androgynous), and worst performance was achieved for class 4 (undifferentiated). Exact discrete confidence intervals for sensitivity could be obtained for each class category.^{41,42}

We believe ODA should be considered the preferred statistical approach vs. alternative methods since it avoids statistical assumptions required of conventional models, is insensitive to skewed data or outliers, and has the ability to handle any variable metric including categorical, Likert-type integer, and real number measurement scales.³¹ Compared to other methods, only ODA can identify the optimal (maximum-accuracy) assignments (categorical attributes) or cutpoints (ordered attributes) which exist for the attribute, that in turn facilitates use of measures

of predictive accuracy. ODA can evaluate model reproducibility using multiple methods, allowing assessment of potential cross-generalizability of the model when applied to classify independent random samples.³¹ We therefore recommend that researchers employ the ODA framework to evaluate the statistical hypotheses which are explored in their laboratory and field research endeavors.⁴³⁻⁶¹

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Author Notes

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