

Implementing ODA from Within Stata: Directional Hypothesis, Multicategorical Class Variable, Ordinal Attribute

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This paper describes how to assess a confirmatory (directional) hypothesis for a design involving a multicategorical class (“dependent”) variable and an ordinal attribute (“independent variable”) using the new Stata package for implementing ODA.

Recent papers¹⁻¹⁹ introduce the new Stata package called **oda**²⁰ for implementing ODA from within the Stata environment. Because this package is a wrapper for the MegaODA software system²¹⁻²³, the MegaODA.exe file must be loaded on the computer for the **oda** package to work (MegaODA software is available at <https://odajournal.com/resources/>). To download the **oda** package, at the Stata command line type: “ssc install oda” (without the quotation marks). This paper demonstrates use of the **oda** package to evaluate the *a priori* hypothesis for a design involving a four-category class variable and equivalent four-category ordinal attribute.

Methods

Data

As an example of a directional hypothesis involving a multicategorical class variable and an ordinal attribute, consider Bishop, Feinberg and Holland’s data²⁴ concerning visual acuity of left

and right eyes for a sample of 7,477 women undergoing eye exams. Unaided distant visual acuity was assessed separately for each eye using a 4-point ordinal scale with 1=acuity $\leq 25^{\text{th}}$ percentile; 2=acuity $\leq 50^{\text{th}}$ percentile; 3=acuity $\leq 75^{\text{th}}$ percentile; and 4=acuity $\leq 100^{\text{th}}$ percentile. The directional alternative hypothesis being tested is that since a person’s eyes tend to have comparable visual acuity, the right eye acuity (randomly selected to serve as class variable) should be directly discriminable on the basis of the left eye acuity.

Analytic Process

The directional (“one-sided”) *a priori* hypothesis is left and right eyes have the same visual acuity rating, and the null hypothesis is that this is not true. Exact *p* is estimated by a 25,000-iteration permutation test. For the entire sample, **oda** is implemented with the following syntax (see the help file for **oda** for a complete description of syntax options):

```
oda righteye lefteye , pathoda("C:\ODA\")
store("C:\ODA") iter(25000) dir(< 1 2 3 4)
```

This syntax is explained as follows: “righteye” is the *class* variable and “lefteye” is the *attribute*; “C:\ODA\” is the directory path where the MegaODA.exe file exists on the computer, and where all other files generated in analysis are stored; the number of iterations (repetitions) used to compute a permutation *p*-value is 25,000; the attribute (righteye) is ordered (default); and the directional hypothesis is that visual acuity code assignments of the left and right eye agree. Data for each observation was entered in free format on a separate line in space-delimited text (ASCII) characters.^{25,26}

The **oda** package produces an extract of the total output produced by the ODA software (the complete output is stored in the specified directory with the extension “.out”).

```
ODA model:
-----
IF LEFTEYE <= 1.5 THEN RIGHTEYE = 1
IF 1.5 < LEFTEYE <= 2.5 THEN RIGHTEYE = 2
IF 2.5 < LEFTEYE <= 3.5 THEN RIGHTEYE = 3
IF 3.5 < LEFTEYE THEN RIGHTEYE = 4

Summary for Class RIGHTEYE Attribute LEFTEYE
-----

Performance Index          Train
-----
Overall Accuracy           70.83%
PAC RIGHTEYE=1             76.92%
PAC RIGHTEYE=2             67.02%
PAC RIGHTEYE=3             72.15%
PAC RIGHTEYE=4             62.36%
Effect Strength PAC        59.48%
PV RIGHTEYE=1              79.71%
PV RIGHTEYE=2              68.05%
PV RIGHTEYE=3              70.68%
PV RIGHTEYE=4              58.50%
Effect Strength PV         58.98%
Effect Strength Total      59.23%

Monte Carlo summary (Fisher randomization):
-----
Iterations: 25000
Estimated p: 0.000000
```

The effect strength for sensitivity (ESS) is labelled in the output as the “Effect Strength PAC” (Percentage Accurate Classification). As seen, ESS for the *a priori* hypothesis is 59.48%, which corresponds to a relatively strong effect²⁵ and has permutation $p < 0.00001$.

In summary, ODA identified a relatively strong model which supported the *a priori* hypothesis that one’s left and right eyes tend to exhibit comparable visual acuity.

We believe ODA should be considered the preferred statistical approach over other methods because it avoids statistical assumptions required of conventional models, is insensitive to skewed data or outliers, and has the ability to handle any variable metric including categorical, Likert-type integer, and real number measurement scales.²⁵ In contrast to alternative methods, only ODA can identify the optimal (maximum-accuracy) assignments (categorical attributes) or cutpoints (ordered attributes) that exist for the attribute, which in turn facilitates the use of measures of predictive accuracy.

Furthermore, ODA can evaluate model reproducibility by multiple methods, allowing assessment of potential cross-generalizability of the model applied to classify an independent random sample.²⁵

For these reasons we recommend that researchers employ ODA and CTA frameworks to evaluate the statistical hypotheses which are explored in their laboratory and field research endeavors.²⁷⁻⁴⁶

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Author Notes

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