

# Value-Added by ODA vs. Chi-Square

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Beyond identifying the *most accurate* classification model which exists for the sample, and estimating *cross-generalizability* vis-à-vis jackknife, hold-out and/or other validity methods, ODA provides the *exact* one- or two-tailed *P*-value, the *sensitivity* and *predictive value* for each category of the class variable, and the *effect strength* corrected for chance.

Contrasts of inherent theoretical limitations of chi-square analysis vs. corresponding strengths of ODA and CTA are well documented.<sup>1-23</sup> It is likewise imperative to emphasize that ODA and CTA are also the analytic methods of choice in seemingly straightforward applications—for example, if data for a truly qualitative attribute satisfy the minimum expectation criterion and one obvious underlying solution exists.<sup>24-27</sup>

This note illustrates the value added by using ODA in analysis for an example of the latter case. For example consider a recent study of gully erosion, in which a complex sampling and interviewing methodology yielded the data in Table 1 on type of adjustment made by the respondent, and if adjustment was individually- or community-motivated.<sup>28</sup> Chi-square=265.0 (df=3, n=720,  $p<0.0001$ ) finds a statistically significant relationship between adjustment and motivation. Chi-square critical value for  $p<0.05$  in this application is 7.82: every cell in the table contributes a value greater than this to omnibus chi-square. It was concluded: “local population driven by self-responsibility relies on individual as well as community-led adjustment measures to ensure their continued survival and habitation in their ancestral homes” (p. 6).

Table 1: Individual- vs. Community-Led Adjustments in Response to Gully Erosion<sup>28</sup>

<u>Adjustment</u>	<u>Individual</u>	<u>Community</u>
Use of Ridges	85	173
Shifting Habitation	65	170
Relocation	172	10
Intensified Cultivation	45	0

MegaODA software<sup>29-32</sup> was employed to discriminate source of motivation (individual vs. community, treated as a class variable) as a function of type of adjustment (multicategorical attribute). The resulting ODA model was:

*If* Adjustment=Use of Ridges or Shifting Habitation, *then predict* Motivation=Community-Led;

*Otherwise*

*If* Adjustment=Relocation or Intensified Cultivation, *then predict* Motivation=Individual-Led.

Using the ODA model to classify the sample data yielded the confusion matrix presented in Table 2.

Table 2: Confusion Matrix for ODA Model, for Training and LOO Results (Sens=Sensitivity; PV=Predictive Value)

Actual Motivation	Predicted Motivation		Sens
	<i>Individual</i>	<i>Community</i>	
<i>Individual</i>	217	150	59.1
<i>Community</i>	10	343	97.2
<u>PV</u>	95.6	69.6	

Because 50% correct classification of each motivation category is expected by chance, model classification of community-motivated adjustments is  $(97.2/50 - 1) \times 100\%$  or 94.4% greater than expected by chance, and classification of individually-motivated adjustments is 18.2% greater than expected by chance: this is greater than a 5-fold difference in accuracy. The finding is thus dominated by the near-uniform response to community-based adjustments.

The Effect Strength for Sensitivity or ESS index of classification accuracy, computed as a function of mean sensitivity achieved by the model across class categories, is used to norm classification accuracy: ESS=0 is the level of accuracy expected by chance, ESS=100 is perfect errorless classification, and ESS<0 is accuracy worse than expected by chance.<sup>1,26,27</sup> Here, ESS=56.3. The rule-of-thumb used to qualitatively assess classification accuracy achieved by a model was based on billions of Monte Carlo experiments: ESS<25 is a relatively weak effect; ESS<50 is a moderate effect; ESS <75 is a relatively strong effect; ESS<90 is a strong effect; and greater values of ESS reflect a very strong effect.<sup>26,33</sup>

Finally, ESS indicates the ability of the ODA model to correctly classify all members of all class categories for the entire sample, while the Effect Strength for Predictive Value or ESP index assesses the accuracy of the model when it is used to make point predictions into a class category (ESS is invariant over base-rate, ESP is not<sup>26</sup>). As seen (Table 2), presently the ODA

model is >95% accurate when classifying an individual motivation, and almost 70% accurate when classifying a community motivation.<sup>34-36</sup>

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#### **Author Notes**

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