

Using ODA to Ascertain if Stratification Yields Different Transition Matrices

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When a first-order Markov model cannot be confirmed one approach is subdividing the sample into strata each having a distinct set of transition probabilities. This note demonstrates the use of ODA to assess whether stratification resulted in significantly different transition matrices.

Data for exposition (Table 1) were drawn from a study of social class identification, and used to illustrate Goodman’s chi-square procedure for testing the hypothesis that sample stratification created dissimilar transition matrices.¹

Table 1: Turnover Data¹ Used to Evaluate Stratified Transition Matrix Dissimilarity

	<u>Better Financial Change in 1958</u>	
	Middle	Working
Middle (1956)	93	23
Working (1956)	26	95

	<u>Worse Financial Change in 1958</u>	
	Middle	Working
Middle (1956)	28	22
Working (1956)	7	66

As described by Markus¹ “Comparing the two Middle Class rows, chi-square (df=1)=10.33 ($p<0.01$); and for the two Working Class rows, chi-square (df=1)=14.90 ($p<0.01$). Thus,

the stratification of the sample by perceived financial change has resulted in significantly different transition matrices” (p. 16).

ODA offers an exact nonparametric analogue to Goodman’s test in this application.²⁻⁷ As in Goodman’s method, two ODA analyses are used, but individual ODA results are considered separately (ESS values aren’t summed). In both analyses Class (Middle vs. Working) is the two-category class variable and perceived financial change is treated as a categorical attribute (this is consistent with chi-square analysis, and treating the attribute as ordered didn’t alter the findings). Results are summarized in Table 2.

Table 2: ODA Stratification Effect Tests

Class	<u>Model Sensitivity</u>		ESS	$p<$
	Middle	Working		
Middle	80.2	44.0	24.2	0.0018
Working	21.5	90.4	11.9	0.045

As seen, ODA revealed relatively weak (defined² as $ESS<25$) statistically significant

discrimination between stratified transition matrices, thus offering moderate support for the hypothesis that stratification by perceived financial change yielded significantly different transition matrices.

References

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Author Notes

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