

Novometrics vs. Yule’s Q: Voter Turnout and Organizational Membership

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A popular legacy index of association for 2x2 tables that is based on the odds ratio (OR), Yule’s $Q = (OR - 1) / (OR + 1)$. Yule’s Q ranges between -1.00 and 1.00, with the value 0 indicating no association. Prior research¹ assessing the association between voting behavior (0=not a voter; 1= voter) and the number of one’s organizational memberships (0=no memberships; 1=at least one membership) reported that $Q = 0.434$, and “...the odds of voting among persons belonging to organizations (is) more than 2.5 times greater than the voting odds among those respondents without memberships” (p. 11). These data were analyzed using exploratory novometrics, treating voting behavior as a class variable and number of organizational memberships as an ordered attribute.²⁻⁴

Data analyzed herein are presented in Table 1.

Table 1: Study Data¹

<i>Voting Behavior</i>	<i>Number of Organizational Memberships</i>	
	<u>None</u>	<u>One or More</u>
<u>Voted</u>	298	689
<u>Did not Vote</u>	254	232

For these data a single optimal model emerged: if number of memberships=none, then predict did not vote; otherwise predict voted: relatively weak $ESS = 22.01$, $D = 7.09$, $p < 0.001$. Reversing the direction of the optimal model yields $ESS = -22.07$ (i.e., relatively weakly worse than is expected by chance).²

Table 2 is the confusion matrix for the optimal model, which correctly classified the

behavior of 7 in 10 of the actual voters, vs. 1 in 2 of the actual non- voters (50% is expected by chance for each of the class categories²).

Table 2: Confusion Matrix for Optimal Model

<u>Actual</u>		<u>Predicted</u>		
		Voter	Non-Voter	
<u>Actual</u>	Voter	689	298	69.8%
	Non-Voter	232	254	52.3%
		74.8%	46.0%	

The confusion matrix also shows that in making point-predictions of voting behavior of individual observations, the model was correct 3 in 4 times it predicted a subject voted, vs. 1 in 2 times it predicted a subject did not vote.

Like kappa, phi, and numerous other legacy measures of association, Yule’s Q is

susceptible to analytic anomalies if one of the “not voted” or “negative” cells is empty, inducing division by zero in methods involving manipulation of the OR.^{1,2,5}

References

¹Knoke D, Burke PJ (1980). *Log-linear models*. Beverly Hills, CA: Sage (pp. 8-11).

²Soltysik RC, Yarnold PR (2010). Automated CTA software: Fundamental concepts and control commands. *Optimal Data Analysis, 1*, 144-160.

³Yarnold PR, Bryant FB (2015). Obtaining an enumerated CTA model via automated CTA software. *Optimal Data Analysis, 4*, 54-60.

⁴Yarnold PR, Soltysik RC (2016). *Maximizing predictive accuracy*. Chicago, IL: ODA Books. DOI: 10.13140/RG.2.1.1368.3286

⁵Yarnold PR (2016). ODA vs. π and κ : Paradoxes of kappa. *Optimal Data Analysis, 5*, 160-161.

Author Notes

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